

Tint Reuven

Number Theorist, Israel

**TO THE HYPOTHESIS OF BILL
(ELEMENTARY ASPECT)**

Summary. *Some equations and equal equations are given. To the hypothesis of Bill.*

Key words: *equations, equalities, Beal's conjecture*

1.

$$\begin{aligned} 1) 3^2 \cdot 3^2 + 3^2 \cdot 2^4 = 3^2 \cdot 5^2 \quad 2) 3^2 \cdot 5^2 + 3^4 \cdot 2^4 = 3^2 \cdot 13^2 \quad 3) 3^4 \cdot 5^2 + 3^2 \cdot 2^6 = 3^2 \cdot 17^2 \\ 4) 3^4 \cdot 7^2 + 3^6 \cdot 2^6 = 3^4 \cdot 5^4 \quad 5) 5^2 \cdot 3^4 + 5^4 \cdot 2^6 = 5^2 \cdot 41^2 \quad 6) 5^2 \cdot 3^2 + 5^2 \cdot 2^4 = \\ 5^4 \quad 7) 5^4 \cdot 3^2 + 5^2 \cdot 2^6 = 5^2 \cdot 17^2 \end{aligned}$$

$$\begin{aligned} 1) 9^2 + 12^2 = 15^2 \quad 2) 15^2 + 36^2 = 39^2 \quad 3) 45^2 + 24^2 = 51^2 \quad 4) 63^2 + 216^2 = 225^2 \\ 5) 45^2 + 200^2 = 205^2 \quad 6) 15^2 + 20^2 = 25^2 \quad 7) 75^2 + 40^2 = 85^2 \end{aligned}$$

2. *We show that equalities with this property are innumerable (without using the previous equalities, since the use of: multiplication of equalities by the corresponding prime numbers in an arbitrary even degree is trivial). Examples: $(13p^9)^2 + (7p^6)^3 = (2p^2)^9$, $(2p^6)^7 + (17p^{14})^3 = (71p^{21})^2$ etc., (when the base is known), $2 \cdot 3^2 = 18$ – least common multiple, $7 \cdot 3 \cdot 2 = 42$ – least common multiple, - the least common multiple, p is an arbitrary prime (or other) number.*

2.1 Basics of the following equalities:

$$\begin{aligned} 7^2 + 2^5 = 3^4, \quad 3^5 + 10^2 = 7^3, \quad 3^5 + 11^4 = 122^2: 2^4 \cdot 7^2 + 2^3 \cdot 2^6 = 2^4 \cdot 3^4 \\ 28^2 + 8^3 = 6^4, \quad 2 \cdot 2 \cdot 3^5 + 2^3 \cdot 5^2 = 2 \cdot 7^3, \quad 2 \cdot 3^5 + 2 \cdot 11^4 = 2^3 \cdot 61^2, \text{ etc. etc.} \end{aligned}$$

3. We have an equation $(A \cdot p^b)^a + (B \cdot p^a)^b = p \cdot p^{ab} = p^{ab+1}$ (1),
if $A^a + B^b = p$ (2), when $A = 2, B$ – arbitrary odd primes, a, b – arbitrary positive integers such that p is a prime number.

Example: $A=2, B=3, a=5, b=4. (2 \cdot 113^4)^5 + (3 \cdot 113^5)^4 = 113^{21},$
 $(2 \cdot 5^4)^5 + (3 \cdot 5^5)^4 = 113 \cdot 5^{20}.$

3.1 If $A=2p_1$, when p_1 – arbitrary prime number not equal B , then the basis for example $(2 \cdot 3)^3 + 7^4 = 2617$ – prime number, and $(2 \cdot 3^5)^3 + (7 \cdot 3^3)^4 = 2617 \cdot 3^{12}$. In general: $(2 \cdot p_1^{b+1})^a + (B \cdot p_1^a)^b = p \cdot p_1^{ab}$ (3).

4. It seems that (2) and (3) have countless solutions.

References

1. Tint R. The proof of Bill's conjecture is a consequence of the properties of invariant identity certain type (elementary aspect) // International Scientific Journal. Kiev, 2016. N11 (21). Vol. 1. <https://doi.org/10.21267/IN.2016.3571>